

8.13

*Oil with an absolute viscosity of  $0.16 \text{ N}\cdot\text{s}/\text{m}^2$  and a density of  $925 \text{ kg}/\text{m}^3$  is flowing in a 200-mm-diameter pipe at  $0.50 \text{ L}/\text{s}$ . How much power is lost per meter of pipe length?*

SI

$$\text{Eq. 4.7: } V = (0.00050)/(\pi 0.200^2) = 0.01592 \text{ m/s}$$

$$\text{Eq. 8.1: } R = [0.20(0.01592)925]/0.16 = 18.40, \text{ flow is laminar. Eq. 8.29: } f = 64/18.40$$

$$\text{Eq. 8.14: } h_f/L = (64/18.40)(1/0.20)0.01592^2/[2(9.81)] = 0.0001796 \text{ meter per meter}$$

$$\text{Eq. 5.41: Power loss} = (925 \times 9.81)(\pi 0.100^2)0.01592(0.0001796) = 0.000815 \text{ watts per meter} \quad \blacktriangleleft$$

8.14

Water at  $50^{\circ}\text{F}$  enters a pipe with a uniform velocity of  $U = 14$  fps. (a) What is the distance at which the transition occurs from a laminar to a turbulent boundary layer? (b) If the thickness of this initial laminar boundary layer is given by  $4.91\sqrt{\nu x/U}$  (from Eq. 9.10), what is its thickness at the point of transition?

BG

Table A.1 for water at  $50^{\circ}\text{F}$ :  $\nu = 1.410 \times 10^{-5}$  ft<sup>2</sup>/sec

(a) Sec. 8.10: At transition point (turbulent boundary layer begins): For  $R_x = 500,000 = Ux/\nu$

$$x = 500,000 \nu / U = 500,000(0.0000141)/14 = 0.504 \text{ ft} = 6.04 \text{ inches} \quad \blacktriangleleft$$

(b) Given:  $\delta = 4.91\sqrt{\nu x/U} = 4.91\sqrt{0.0000141 \times 0.504/14} = 0.00350$  feet or 0.0420 inches  $\blacktriangleleft$

In a 36-in-diameter pipe velocities are measured as 18.5 fps at  $r = 0$  and 18.0 fps at  $r = 4.0$  in. Approximately what is the flow rate?

Eq. 8.40:  $18.0 = 18.5 - 5.76u_* \log[18/(18 - 4.0)]$  from which  $u_* = 0.795$  fps

Eq. 8.37:  $0.795 = u_* = V\sqrt{f/8}$ . Thus  $f^{1/2} = 2.25/V$  (1)

Eq. 8.43:  $V/18.5 = 1/(1 + 1.326f^{1/2})$  (2)

Eliminating  $f$  between (1) and (2):  $\frac{18.5}{V} = 1 + 1.326\frac{2.25}{V}$ , from which  $V = 15.52$  fps (so  $f = 0.0579$ )

Eq. 4.7:  $Q = AV = (\pi/4)(36/12)^2 15.52 = 109.7$  cfs ◀

8.18

Water at 60°C flows in a 15-mm-diameter copper tube ( $e = 0.0015$  mm) at 0.06 L/s. Find the head loss per 10 m, using Eq. (8.29) or (8.52) to find  $f$ . What is the centerline velocity, and what is the value of  $\delta_v$ ?

SI

Table A.1: At 60°C,  $\nu = 0.474 \times 10^{-6}$  m<sup>2</sup>/s

$$\text{Eq. 4.7: } V = Q/A = \frac{4Q}{\pi D^2} = \frac{4(0.06 \times 10^{-3})}{\pi(0.015)^2} = 0.340 \text{ m/s}$$

$$\text{Eq. 8.1: } R = \frac{DV}{\nu} = \frac{0.015(0.340)}{0.474 \times 10^{-6}} = 10\,740 \text{ (flow is turbulent); } \frac{e}{D} = \frac{0.0015}{15} = 0.000100$$

$$\text{Eq. 8.52: } f = 0.0304; \quad \text{Eq. 8.13: } h_f = 0.031 \frac{10}{(0.015)^2} \frac{0.340^2}{2(9.81)} = 0.1191 \text{ m} \quad \blacktriangleleft$$

$$\text{Eq. 8.43: } 0.340/u_{\max} = 1/[1 + 1.326(0.0304)^{1/2}]; \quad u_{\max} = 0.418 \text{ m/s} \quad \blacktriangleleft$$

$$\text{Eq. 8.38: } \delta_v = \frac{14.14(0.474 \times 10^{-6})}{0.340(0.0304)^{1/2}} = 0.0001132 \text{ m} \quad \blacktriangleleft$$